

Statements about possible future climate change are usually based on ensembles of model simulations. But, the question rises how many simulations are adequate to derive a robust assessment of the bandwidth of a climate change signal?

Let's assume that an available large ensemble of simulations represents the "knowledge" of climate changes bandwidth. The goal of the introduced method is to **determine the minimum ensemble size of a drawn random sample, which still obtain a reliable bandwidth of the full ensemble.**

Method

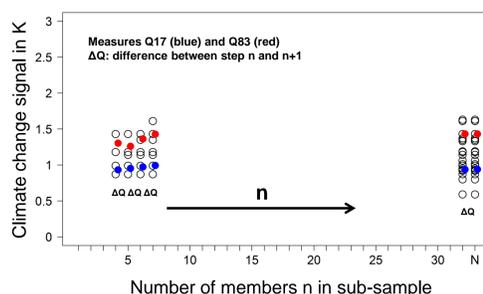
Method: Testing the convergence of the range of climate change, while the size of the drawn sample is enlarged successively

First, a measure has to be defined, representing the bandwidth of climate change of a special quantity. Here the quantiles Q17 and Q83 are used to represent the characteristic of the full ensemble according to the "likely"-range of 66% in the IPCC report.

Results analyzing a trial ensemble of 33 simulations (mixed RCP and SRES scenarios) of 2m-temperature 50 year climate change signals over Germany are shown here.

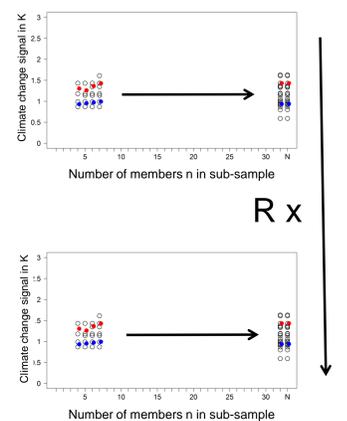
1. Procedure

- A sample of n elements (starting with 4) is drawn randomly with replacement from the full ensemble
- Enlarge successively the drawn sample by 1 element up to the total number N
- Compute the measures Q17 and Q83 for all $n=4, \dots, N$
- Compute the difference ΔQ of Q17 and Q83 between all steps n and $n+1$
- For all steps $n \rightarrow n+1$: test, whether ΔQ exceeds a criterion ϵ (e.g. 5% of median). If $\Delta Q < \epsilon$, the range of the full ensemble is sufficient reproduced.



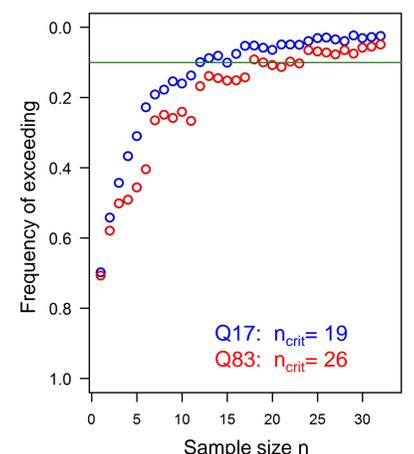
2. Resampling

- The procedure is repeated R -times
- Count the number of exceedances U_n for each step



3. Test

- Test, if the frequency of exceeding U_n is smaller than a value allowed (e.g. $V_{crit} = 10\%$) for each step
- The smallest step $n=n_{crit}$ where the condition $U_n < V_{crit}$ is fulfilled for this and all following steps is the minimum ensemble size which represents the full ensemble bandwidth.



Dependency on parameters

The minimum ensemble size n_{crit} depends on parameters, which have to be defined:

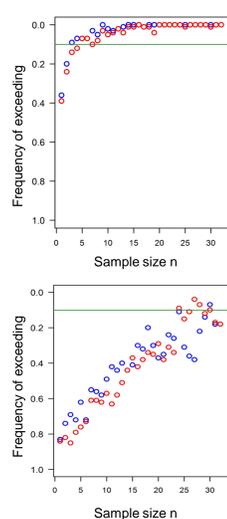
Measure: range of climate change, e.g. quantiles Q17 and Q83

criterion ϵ : for the difference between step n and $n+1$, e.g. 5% of median

frequency of exceeding allowed: e.g. $V=10\%$

The figures on the right side show results for two artificial examples with different width of the distribution function.

If a higher accuracy of the reproduced range is required, the parameters ϵ and V have to be set to smaller values. So, the range converges later (or never) and more simulations are needed.



Outlook

Up to now just climate 30-year means are used as input data. A further resampling step will be included to introduce the effect of internal variability into the consideration. For this, the 30-year means will be computed by drawing (with replacement) 30 single annual means out of the original data.

ReKliEs-De project: investigate a large ensemble RCP8.5-driven simulations from EURO-CORDEX framework and additional simulations conducted in the ReKliEs-De project.